

Half-Lives of Radioactive Isotopes

Transmutation

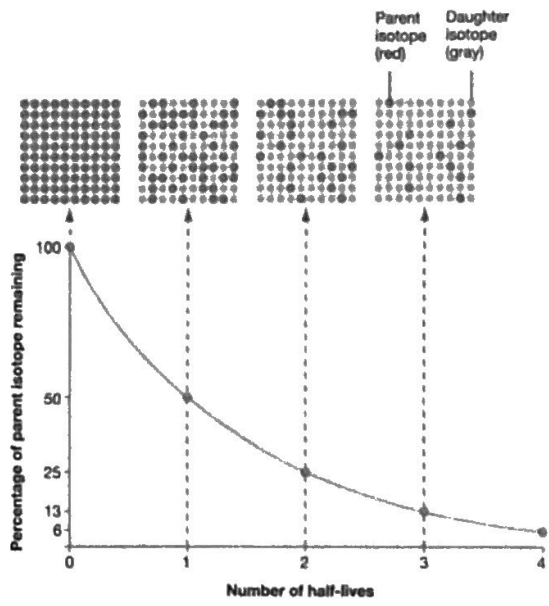
- In (natural) transmutation, the nucleus spontaneously decays into a new element.

$${}^{226}_{88}\text{Ra} \rightarrow {}^{222}_{86}\text{Rn} + {}^4_2\text{He}$$
- In artificial transmutation, the nucleus is first bombarded with high energy particles, then decays and changes into a new element.

$${}^{27}_{13}\text{Al} + {}^4_2\text{He} \rightarrow {}^{30}_{15}\text{P} + {}^1_0\text{n}$$

Half-Life

- Every radioisotope has a rate of decay.
- Half-life is the time it takes for half of a sample to decay into a new element
- Table N lists half-life, decay mode (particles emitted during decay), nuclide (radioisotope, and name of nuclide).
- The half-life of Ra-226 is 1600 years; meaning, in 1600 years half of Ra-226 will decay, and in another 1600 years half of what was remaining will decay.
- After 3200 years, how many half-lives has Ra-226 gone through?
2 Half lives



Common Radioisotopes

- Carbon-14 (C-14) has a half-life of 5700 years and is used to date once living (organic) material
- Uranium-238 (U-238) has a half-life 4.5 billion years and is used to determine the age of rock
- Iodine-131 (I-131) has a half-life 8.021 days and is used for treatment of thyroid disorders
- Cobalt-60 (Co-60) has a half-life 5.271 years and is used for cancer treatments

Fraction Remaining

- ${}^{131}_{53}\text{I}$ has a half-life of 8.07 days. A 10 gram sample was allowed to decay for 32 days. What fraction will remain?

$\frac{32}{8.07} = 4 \text{ H.L.}$ $1 \rightarrow \frac{1}{2} \rightarrow \frac{1}{4} \rightarrow \frac{1}{8} \rightarrow \frac{1}{16}$

1 H.L. 2 H.L. 3 H.L. 4 H.L.

$\frac{1}{16}$ remains

What is the Half-Life?

- 100 grams of a radioisotope decayed to 12 1/2 grams after 90.7 years. What was the half-life?

$100\text{g} \rightarrow 50\text{g} \rightarrow 25\text{g} \rightarrow 12.5\text{g}$

90.7 years

3 H.L. in 90.7 years

$\frac{90.7}{3} = \boxed{30.2 \text{ years} = 1 \text{ H.L.}}$

What was the Initial Amount (Original Amount)

- A radioisotope has a half-life of 10 days. 1 gram remains after 40 days. What was the initial amount of the radioisotope?

HL = 10 days

$\frac{40 \text{ days}}{10 \text{ days}} = 4 \text{ H.L.}$

(work backward)

16g → 8g → 4g → 2g → 1g

4 H.L. 3 H.L. 2 H.L. 1 H.L.

16g
initial amount

More - Mixed Half-Life Practice

1. How long will it take for 30 g of ^{222}Rn to decay to 7.5 g?

HL = 3.823 day (Table N) | 30 → 15 → 7.5 | 2 H.L. | 2(3.823) = **7.646 days**

$\xrightarrow{1 \text{ H.L.}}$ $\xrightarrow{2 \text{ H.L.}}$

2. How many grams of ^{16}N will be left from a 16 g sample after 21.6 s?

HL = 7.13 s (Table N) | $\frac{21.6}{7.13} = 3 \text{ H.L.}$ | 16g → 8g → 4g → 2g | **2 grams**

$\xrightarrow{1 \text{ H.L.}}$ $\xrightarrow{2 \text{ H.L.}}$ $\xrightarrow{3 \text{ H.L.}}$

3. How many half-lives will it take for 50 g of ^{99}Tc to decay to 6.25 g?

50g → 25g → 12.5g → 6.25g | **3 Half lives**

$\xrightarrow{1 \text{ H.L.}}$ $\xrightarrow{2 \text{ H.L.}}$ $\xrightarrow{3 \text{ H.L.}}$

4. What fraction of a sample of ^{32}P will be left after 42.9 d?

HL = 14.28 days (Table N) | $\frac{42.9}{14.28} = 3 \text{ H.L.}$ | 1 → $\frac{1}{2}$ → $\frac{1}{4}$ → $\frac{1}{8}$ | **$\frac{1}{8}$ remains**

$\xrightarrow{1 \text{ H.L.}}$ $\xrightarrow{2 \text{ H.L.}}$ $\xrightarrow{3 \text{ H.L.}}$

Regents Questions

1. Which radioisotopes have the same decay mode and have half-lives greater than 1 hour?

- TABLE N
- (B) a. Au-198 and N-16 $Au = 2.695 \text{ d} / \beta^-$ $N = 7.13 \text{ s} / \beta^-$
 - b. I-131 and P-32 $I = 8.021 \text{ d} / \beta^-$ $P = 14.28 \text{ d} / \beta^-$
 - c. Ca-37 and Fe-53
 - d. Tc-99 and U-233 $Tc = 2.13 \times 10^5 \text{ y} / \beta^-$ $U = 1.592 \times 10^8 \text{ y} / \alpha$

2. After decaying for 48 hours, 1/16 of the original mass of a radioisotope sample remains unchanged.

What is the half-life of this radioisotope? **48 hours**

(C) a. 3.0 h

b. 9.6 h

c. 12 h

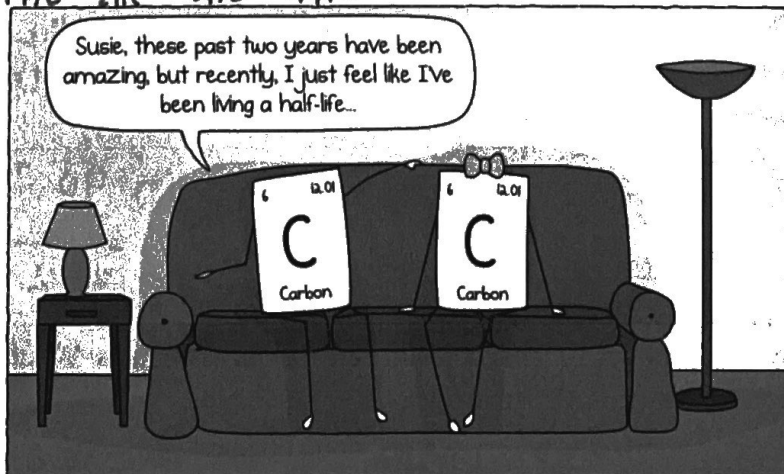
d. 24 h

1 → $\frac{1}{2}$ → $\frac{1}{4}$ → $\frac{1}{8}$ → $\frac{1}{16}$

$\xrightarrow{1 \text{ HL}}$ $\xrightarrow{2 \text{ HL}}$ $\xrightarrow{3 \text{ HL}}$ $\xrightarrow{4 \text{ HL}}$

48 hours
4 H.L.

$\frac{48}{4} = 12 \text{ hours}$



c. Ca-37 & Fe-53

Ca = 182 ms / β^+

Fe = 8.51 min / β^+